Calcium carbonate scales on process equipment:
A measure of the induction time for nucleation

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ABSTRACT
Scale deposition on process equipment surfaces has several disadvantages: in particular, when scales crystallize on heat transfer surfaces, they offer a resistance to the heat flow and can accumulate in pipelines, orifices and other flow passages seriously impeding the process flow. Moreover, calcium carbonate scales, together with calcium sulfate scales, are the major cause of fouling in reverse osmosis membranes, resulting in a continuous decline in desalted water production thus reducing the overall efficiency and increasing operation and maintenance costs. Therefore, from an economic point of view, the formation of these mineral scales is an obstacle to the recovery of potable water from sea or brackish waters as well as to the industrial utilization of many natural waters. The aim of the paper is to measure the induction time for calcium carbonate precipitation, through a well-assessed laser light scattering technique previously devised. Experiments are carried in a batch thermostated reactor at room temperature, pH in the range 7–8, in a supersaturation range from 2 to 200. The induction time so measured could be used to estimate thermodynamic parameters such as the interfacial tension between crystals and mother suspension. The knowledge of interfacial tension is of major importance for guiding the choice of the most suitable additive for the inhibition of CaCO$_3$ scale formation.

Keywords: Nucleation; Induction period; Calcium carbonate; Scale

1. Introduction
Calcium carbonate is, together with calcium sulphates, the main component of scales on process equipment surfaces. Their presence is mostly unwanted in several industrial applications, since scales reduce heat and mass transfer coefficients.

As for example, water desalination by membrane process is hindered by the presence of bicarbonates dissolved in raw water, which following warming of the feed decompose and carbonates precipitate on the membrane surface. Scaling causes a progressive wettability of the membrane, and as a result, the decline of both the permeate flux and the separation efficiency was observed [1–5]. Alkaline scales such as calcium carbonate can be controlled by maintaining pH below 7.5 with acidification. If sulfuric acid is added for pH control due to its low cost, the potential of calcium-sulfate scale formation is increased. Moreover, sulfuric acid can also cause system corrosion, which in turn can be an additional source of fouling. Thus, an ideal scale inhibitor would be able to prevent both calcium-carbonate precipitation at high pH and calcium-sulfate precipitation at low pH (neutral or slightly acidic) [6].

The study of the effects of an additive on nucleation can be carried out by evaluating the induction period ($t_{\text{ind}}$), defined as the time elapsing between the onset of supersaturation and the formation of critical nuclei, or embryos [7–13].

The various experimental techniques detect with a different resolution the first portions of the crystalline phase, that nucleates and grows in a supersaturated solution. As a result, under otherwise equal conditions, induction time may not have the same value when measured by different techniques. However, this time primarily depends on solution supersaturation and temperature and it is the sum of two components: nucleation time ($t_n$), related to the appearance of the critical nuclei, and growth time ($t_g$), connected to the growth process, leading from critical nuclei to measurable crystals. Depending on the relative values of these two time periods, induction time can be influenced by nucleation alone ($t_n \gg t_g$, nucleation-controlled induction period), by both mechanisms ($t_n \approx t_g$, nucleation-and-growth-controlled induction period) or by growth alone ($t_n \ll t_g$, growth-controlled induction period) [14,15]. While $t_g$ can be estimated by a kinetic growth expression, $t_n$ is more difficult to quantify. Nevertheless, it is possible to discriminate whether the appearance of the new solid phase is controlled by nucleation and/or by growth, on the basis of the dependence of $t_{\text{ind}}$ on supersaturation.

In particular, if the process which takes place is truly homogeneous nucleation, i.e. it occurs in a clear solution under the effect of supersaturation alone, $t_{\text{ind}}$ is inversely proportional to the nucleation rate, defined as the number of nuclei formed in solution per unit time and volume.

In this case, as shown by Mullin [16] and Söhnel and Gar-side [17], it is possible to use the experimental knowledge of the induction period to estimate the interfacial tension ($\gamma$) between crystals and the surrounding solution for nucleation based on the dependence of $t_{\text{ind}}$ on supersaturation.

In this paper, preliminary results on calcium carbonate precipitation are reported; through a well-assessed laser light scattering technique previously devised, the induction time is measured at the temperature of 20°C, pH in the range 7–8; the interfacial tension between crystals and mother solution is estimated.

2. Materials and methods

The experimental apparatus consists of a stirred reactor with a related optical device and is schematically shown in Fig. 1. The reactor is a batch cylindrical crystallizer, made of glass, with a working volume of $1.1 \times 10^{-3}$ m$^3$ and a diameter of 0.09 m. The crystallizer is surrounded by a water jacket for temperature control; stirring is provided by a two-blade polypropylene stirrer, with rotation rate ranging between 1 and 10 s$^{-1}$. An off–take tube, placed at half of the working height of the liquid, allows to withdraw samples of the suspension; the position of the tube has been chosen to ensure that the content of the exit stream is the same as the content of the reactor.

The stream removed by the off–take tube is sent, by a peristaltic pump, to an analysis flow–through cell, and then is conveyed again to the crystallizer. The cell, made of quartz, is 0.07 m long, with a square section of $2.5 \times 10^{-5}$ m$^2$ and 0.0025 m thickness. A 10 mW He–Ne laser beam ($\lambda = 632.8$ nm) is focused on the cell, orthogonal to its walls; the beam, whose diameter is 2 mm, is vertically polarized. On the path of the laser beam, placed at 45° with respect to its direction, a beam splitter is provided in order to divide the laser beam into two parts; one is used to illuminate the measure cell, while the other, collected by a photodiode, allows to check the stability and the intensity of the laser beam ($I_0$). The signal of the scattered light ($I_{\text{sca}}$) is collected by two lenses of focal 120 and 50 mm, at 90° with respect to the

Fig. 1. Lab-scale experimental apparatus.
laser beam; this signal is sent, through a quartz optical fiber which ends on an interferential filter, to a photomultiplier tube, connected to a power supply with voltage variable in the range of 0–1000 V. The signal of the transmitted light ($I_{\text{trans}}$) is collected by a photodiode located beyond the cell, at $0^\circ$ with respect to the laser beam. The two analogue signals of scattered and transmitted light, together with $I_o$, are collected by a recorder device.

Supersaturated solutions of calcium carbonate were prepared by mixing clear aqueous solutions of reagent-grade CaCl$_2$·2H$_2$O and NaHCO$_3$ (Applichem, Darmstadt, Germany). All Ca$^{2+}$ ions concentration as CaCO$_3$ was standardized through EDTA titrimetric method.

Once prepared all the solutions were filtered, by using a 0.45 mm filter (Millipore, HVLP 4700) and a vacuum pump (Vacuubrand, MZ4C), in order to eliminate all foreign materials inevitably present in the solution, and then mixed directly into the reactor. The equimolar concentration of CaCl$_2$·2H$_2$O and NaHCO$_3$ in the reactor varied between 2 and 36 mol/m$^3$.

The supersaturation ratio was calculated considering the liquid–solid equilibrium between Ca$^{2+}$ and CO$_3^{2-}$ ions and solid CaCO$_3$, as described by the following equation:

$$\text{Ca}^{2+} + \text{CO}_3^{2-} = \text{CaCO}_3$$

so that it is:

$$S = \frac{a_{\text{Ca}^{2+}}a_{\text{CO}_3^{2-}}}{K_{ps}}$$

where $a_J$ represents the activity of the $J$ species ($J=\text{Ca}^{2+}$, CO$_3^{2-}$) expressed as the product of the molality ($m$) and the activity coefficient ($\gamma_J$), and $K_{ps}$ is the solubility product of calcium carbonate. The value of $K_{ps}$ was calculated as a function of temperature by means of the following relationship [18]:

$$pK_{ps} = 0.001183T + 8.03$$

3. Results and discussion

As already said, preliminary experimental results include tests conducted by setting the temperature at the value $T = 20^\circ$C, with changing the supersaturation $S$ in the range 2–200.

Fig. 2 reports the signal of transmitted light as a function of time for $S = 67$. The figure shows the decrease of the signal with respect to its initial value, with individuating an induction time equal to about 130 s.

Fig. 3 shows all the experimental results, showing the dependence of induction period on supersaturation, at $T = 25^\circ$C.

The experimental data have been linearized according to the following semi-empirical correlation, on which the line reported in Fig. 2 is based on:
where \( K \) and \( r \) are empirical constants \((K = 1.57 \times 10^6, r = 2.32, R^2 = 0.975)\). This figure shows that the induction period for \( \text{CaCO}_3 \) nucleation continuously decreases with increasing supersaturation.

Fig. 4 shows a comparison between calcium carbonate and calcium sulfate dehydrate in terms of the induction times as a function of \( S \). From the figure it is well visible the very different behavior of the two scale forming salts: while induction times for gypsum nucleation spans from few minutes to almost an hour in a very narrow supersaturation range (2–2.7), to have the same \( t_{\text{ind}} \) variations for calcium carbonate it is necessary to increase the supersaturation of two order of magnitude (2–200), at a fixed temperature. In other words, the distance of metastability curve from solubility curve for calcium carbonate appears higher then calcium sulfate dehydrate, that is the width of the metastable zone seems to be wider. This represents an advantage in scaling prevention, since a broad metastable zone would result in a more governable process. However, this circumstance should be confirmed by additional experiments carried out at different temperatures.

As already said, when carried out for a wide range of supersaturation, the experimental measurements of induction time at different supersaturation ratios can be used to estimate the interfacial tension between crystals and mother solution. By considering that the nucleation time is controlled by nucleation, as generally assumed for calcium carbonate crystallization [15], the linearization of the experimental points at \( T = 25^\circ \text{C} \) (Fig. 5) has been conducted according to the following equation, derived from homogeneous nucleation equations when nucleation is the controlling mechanism \((t_n < t_g)\) [17]:

\[
\log(t_{\text{ind}}) = C_N + \frac{D_N}{T^3} \Delta \log(S)
\]

where \( C_N \) is an empirical constant and \( D_N \) is given by:

\[
D_N = \frac{\beta \gamma_s V_m N_A}{(2.3R)^3 \nu^2} f(\phi)
\]

where \( \beta \) is a shape factor, \( \gamma_s \) is the surface energy, \( N_A \) is the Avogadro number, \( R \) is the gas constant, \( V_m \) the molar volume, \( \nu \) is the number of ions in which the molecule is dissociated and \( f(\phi) \) is a correction factor which takes into account the heterogeneous nucleation; in particular, when purely homogeneous nucleation takes place it is \( f(\phi) = 1 \) while when heterogeneous nucleation occurs it is \( f(\phi) < 1 \). Consequently a change in the slope of the equation may indicate a transition from homogeneous to heterogeneous nucleation mechanisms.

The results of the linearization carried out on all \( t_{\text{ind}} \) experimental homogeneous data (in Eq. (6) it was assumed \( \beta = 16\pi/3, \) assuming spherical particle and \( V_m = 36.9 \text{ cm}^3/\text{mol} \); \( R^2 = 0.87 \)) gave the value of \( \gamma_s = 109.3 \text{ mJ/m}^2 \), that is in a good agreement with other available literature values [14–16], thus confirming \textit{a posteriori} the considered nucleation mechanism.

4. Conclusions

In this paper, preliminary results on calcium carbonate crystallization are reported. In details, the induction time for carbonate crystallization has been measured at the constant temperature of 25°C, at a supersaturation ratio ranging from 2 to 200, pH in the range 7–8, by using a laser well...
assessed optical technique. The measured induction times show a strong dependence on supersaturation, from which it will be possible to estimate the interfacial tension between crystals and mother solution. A comparison of two main scale forming salts, calcium carbonate and calcium sulfate dehydrate, has shown that the first seems to have a wider metastable zone. Moreover, from the linearization of the obtained results, the interfacial tension between calcium carbonate crystals and mother solution has been estimated to be $\gamma_{sl} = 109.3 \text{ mJ/m}^2$.

References