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## Comparative analysis of fixed-bed sorption models using phosphate breakthrough curves in slag filter media

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## ABSTRACT

Fixed-bed kinetic sorption (Bohart-Adams, Thomas, Yoon-Nelson, Clark, Wolborska, and modified dose-response) models are commonly used to simulate breakthrough curves (BTCs) from fixed-bed systems. However, more caution should be taken in using these models. Some researchers misused the equation, which is a totally different type from the original model, as a simplified model. Others used the same equation expressed in different forms as an independent model. The aim of this study was to clarify the fixed-bed sorption models via comparative analysis using the phosphate BTCs in slag filter media. For the analysis, the breakthrough data for phosphate (initial phosphate concentration = 1.0 and 2.0 mg/L) sorption in fixed-bed columns (inner diameter = 2.5 cm and column length = 10, 20, and 30 cm) were obtained from the experiments. The original Bohart–Adams model was simplified in the literature to the convergent- and divergent-type models in order to be used for the BTC analysis. However, the divergent-type model, which is equivalent to the Wolborska model, should not be the type of Bohart-Adams model used, because it behaves totally different from the original model. Also, the Thomas and Yoon-Nelson models should not be used simultaneously with the Bohart-Adams model, because they are equivalent to the simplified convergent-type Bohart-Adams model, and the parameters of both of the models  $(k_T, q_0, k_{YN}, and \tau)$  can easily be calculated from the Bohart-Adams model parameters ( $k_{BA}$  and  $N_0$ ). The Bohart-Adams, Clark, and modified dose-response models could describe the BTCs relatively well with a high determination coefficient and a low chisquare coefficient. From this study, the Bohart-Adams, Clark, and modified dose-response models are recommended for the BTC analysis, because these models can provide useful design parameters ( $k_{BA}$ ,  $N_0$ ,  $Z_0$ ,  $t_b$ , and  $q_0$ ) for the fixed-bed systems.

*Keywords:* Breakthrough curves; Fixed-bed kinetic sorption models; Bohart–Adams model; Clark model; Modified dose-response model; Slag filter media

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