Thickness of adsorbed water film in underground gas reservoir

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\begin{abstract}
The bound water is in the form of capillary water and water film in the sand stone of actual gas reservoir underground. According to the Derjaguin–Landau–Verwey–Overbeek (DLVO) theory, the theoretical calculation model of total disjoining pressure and water film thickness is constructed. Combined with the extended Young–Laplace formula, a graphical method for calculating the water film thickness is proposed. The curve of total disjoining pressure and water film thickness is obtained when the actual water salinity and formation temperature and pressure are considered. In actual gas reservoir with high formation water salinity, the electrostatic repulsion is quite small and only the van der Waals force is the main force to keep the water film stable, so the water film thickness in the gas reservoir is small. Comparing the critical pore radius and water film thickness, it shows that the bound water is mainly in the form of capillary water, and the water film thickness is much smaller than the pore radius, which has a limited influence on the percolation of natural gas. The water film thickness is not so important as thought before when evaluating the effective pores in gas reservoir.
\end{abstract}

\textbf{Keywords:} Gas reservoir; Capillary pressure; Disjoining pressure; Bound water; Thickness of water film

1. Introduction

The pore-throat configuration of the reservoir underground is very complicated. The bound water in the inorganic pores of sand stone in gas reservoir underground is mainly in the form of capillary water and water film, which has a great influence on the gas permeability [1–3]. The traditional view was that the water film is formed by the adsorption on the surface of the rock particles, and the pore can be effective seepage channel only if the throat radius is greater than the water film thickness. Since the pore size is quite small usually, the water film thickness was thought to be quite important when evaluating the effective pores in gas reservoir.

Many scholars research on the disjoining pressure and the water film thickness. Derjaguin and Churaev [4] defines the disjoining pressure as a mechanical stress that applied to the bulk liquid with a certain thickness of the liquid membrane that reaches the equilibrium state, and he proposes that the disjoining pressure is composed of the electrostatic force, van der Waals force and structural force. Gee et al. [5] tests the water film thickness of air, deionized water and quartz surfaces at room temperature with elliptical polarization technique. Nishiyama and Yokoyama [6] researches the relationship between the pore size distribution and the water film thickness, and explained the effect of water film on water-rock reaction. Ward et al. [7] quantitatively determines the effect of pH and ionic strength on the film thickness and its stability.

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In this study, a disjoining pressure model is derived considering a combined effect of temperature, pressure, salinity and interfacial tension, which is based on the Derjaguin–Landau–Verwey–Overbeek (DLVO) theory. Moreover, a graphic method of calculating the water film thickness is proposed.

2. Model principle

2.1. Distribution of gas and water in the reservoir

As shown in Fig. 1, the gas generated from kerogen in shale displaces water in neighboring pores. As the pores are water-wet pores, capillary force is the resistance when the gas is driving water. When the capillary force is greater than the pressure difference between gas and water, the gas can effectively displace the original formation water in the pores. The pore radius determines the size of the capillary force, resulting in a very different state of distribution of the aqueous phase as shown in Fig. 2. In smaller pores, the pore is filled with formation water in the form of capillary bound water. In the pore whose radius bigger than certain critical radius \( r_c \), the center of the pore is filled with gas and the formation water covers the pore walls in the form of water film.

The pore network in reservoir is simplified to the capillary bundle model. For the pores at the same depth \( Z \) above the free-water level, the bound water is different due to the difference in the radii of the pores as shown in Fig. 3. At the \( Z \)-level above the gas/water interface, or free water level, in a water wet sand stone in gas reservoir, there is a corresponding critical pore radius \( r_c \), which makes the pressure difference between gas phase and water phase equal to the capillary pressure. As shown in Figs. 3 and 4, in the pores with size of the critical radius \( r_c \), both capillary water and water film exist, which is:

\[
p_c = \frac{2\sigma_{gw}\cos\theta}{r_c} Z
\]

where \( Z \) is the height above the gas–water interface, m; \( \rho_g \) is the gas density, kg/m\(^3\); \( \rho_w \) is the water density, kg/m\(^3\); \( r_c \) is the radius of the critical pore corresponding to the capillary pressure at \( Z \)-position; \( p_g \) is the gas phase pressure, Pa; \( p_w \) is the water phase pressure, Pa; \( \sigma_{gw} \) is the interfacial tension between gas phase and water phase, N/m; \( \theta \) is wetting contact angle, \(^\circ\).

At the same \( Z \)-depth level above the gas/water interface, if the pore radius \( r < r_c \), the pore is filled with capillary water as shown in Figs. 3 and 5. Meanwhile, if the pore radius \( r > r_c \), the center of the pore is filled with gas, and the pore wall is covered by water film as shown in Figs. 3 and 6.

In the hydrodynamic equilibrium state, at different depths above the gas/water interface, the capillary pressure of pores increases with increasing \( Z \) level. The capillary pressure \( p_c \) at certain \( Z \)-level in the formation underground can be determined by following methods:

- If the gradient of gas pressure and water pressure is known, the capillary pressure \( p_c \) can be calculated with Eq. (1), which is the pressure difference between gas and water phase at the same depth.
- Alternatively, if the water saturation at \( Z \)-position above the gas–water interface of is known, the capillary pressure \( p_c \) can be deduced from capillary pressure injection curve.

2.2. Extended Young–Laplace equation

Capillary pressure is defined as the pressure difference between the two-phase interfaces, and the value is equal to the non-wetting phase pressure minus the wetting phase pressure.

\[
p_c = p_g - p_w = \Pi + 2\sigma_{gw}
\]

Fig. 1. Displacement of formation water during gas migration.

Fig. 2. Distribution of fluids in inorganic pores of sand.
where \( p_c \) is capillary pressure, Pa; \( p_g \) is gas pressure, Pa; \( p_w \) is water pressure, Pa; \( \Pi \) is the rejecting pressure between gas/water interface and water/solid interface of the water film, that is, the disjoining pressure, Pa; \( H \) is the mean curvature of solid surface in the water film, 1/m; \( \sigma_{gw} \) is the interfacial tension of gas/water interface, N/m.

The pores network of the reservoir can be reduced to bundle of capillary tubes as shown in Fig. 3. In the capillary tube, Eq. (2) can be rewritten as:

\[
p_c = p_g - p_w = \Pi + \left( \frac{1}{R_1} + \frac{1}{R_2} \right) \sigma_{gw}
\]

(3)

where \( R_1 \) and \( R_2 \) are the principal radius of curvature of the gas/water interface, respectively, m.

The rock pore system can be characterized by a capillary bundle model. In the hydrophilic capillary, there are two types of microscopic water/gas interface [8], which are discussed separately as following:

2.2.1. Gas/water interface in the capillary tube being of spherical concave shape surface

At the spherical concave surface in the capillary tube shown at point \( A \) as shown in Figs. 3 and 4, since the water thickness is quite large, so the disjoining pressure \( \Pi = 0 \). Ignoring the thickness changes of water film transition zone at the gas/water interface, there is:

\[
R = R_2 = \frac{r}{\cos \theta}
\]

(4)

where \( r \) is the capillary radius, m and \( \theta \) is the wet contact angle.

Substituting Eq. (4) into Eq. (3), we get the conventional Laplace formula as:

\[
p_c = p_g - p_w = \frac{2 \sigma_{gw} \cos \theta}{r}
\]

(5)
It is noteworthy that, in the capillary pressure injection test of conventional gas reservoir engineering analysis, the capillary pressure is generally expressed with Eq. (5).

2.2.2. Gas/water interface in the capillary tube being of cylindrical shape surface

As shown in Figs. 4 and 6, in the capillary bundle model, the water film is present in the pores in the form of a columnar liquid surface.

Take the point B in Fig. 4 or the point C in Fig. 6 as an example, since \( R_s = \infty, R_c = r - h \), we can get the following equation from Eq. (3):

\[ p_c = p_g - p_w = \Pi + \frac{\sigma_{gw}}{r - h} \] (6)

Hall et al. [9] argued that \( h \) can be ignored because the water film thickness is quite small compared to the pore size.

2.3. Disjoining pressure of water film on the pore wall

In the pore with the radius \( r \geq r_c \), the relationship between the disjoining pressure of the water film and the capillary pressure is as follows.

2.3.1. In the capillary with the radius \( r = r_c \)

As shown in Fig. 4, when the radius is \( r = r_c \), there is both capillary water and water film in the pore. At the same subsea, there is the following relationship in the hydrodynamic equilibrium state:

\[ p_{gl} = p_{gA}, \quad p_{wl} = p_{wA} \] (7)

where \( p_{gl} \) is the gas pressure close to \( A \) point in gas–water interface, \( p_{gA} \); \( p_{wl} \) is the water pressure close to \( A \) point in gas–water interface, \( p_{wA} \); \( p_{gB} \) is the gas pressure at \( B \) point in gas–water interface, \( p_{gB} \); \( p_{wB} \) is the water pressure close to \( B \) point in gas–water interface, \( p_{wB} \).

According to Eq. (5), there is the following relationship at point \( A \).

\[ p_c = p_{gA} - p_{wA} = \frac{2 \sigma_{gw} \cos \theta}{r_c} \] (8)

According to Eq. (6), there is the following relationship at point \( B \).

\[ p_c = p_{gB} - p_{wB} = \Pi + \frac{\sigma_{gw}}{r_c - h} \] (9)

According to Eqs. (6)–(9), the disjoining pressure of the water film is calculated as follows:

\[ \Pi = p_c \frac{\sigma_{gw}}{r_c - h} = (p_c - p_w)gZ \frac{\sigma_{gw}}{r_c - h} = \frac{2 \sigma_{gw} \cos \theta}{r_c} - \frac{\sigma_{gw}}{r_c - h} \] (10)

where \( h \) is the water film thickness in the equilibrium condition.

2.3.2. In the capillary with the radius \( r > r_c \)

As shown in Fig. 6, there is a water film when the pore radius is \( r > r_c \). According to Eq. (6), the disjoining pressure of the water film at point \( C \) is as follows:

\[ \Pi = p_c - \frac{\sigma_{gw}}{r - h} = (p_c - p_w)gZ \frac{\sigma_{gw}}{r - h} \] (11)

where \( p_{wc} \) is the gas pressure close to \( C \) point in gas–water interface, \( p_{wc} \); \( p_{wc} \) is the water pressure close to \( C \) point in gas–water interface, \( p_{wc} \).

Substituting Eq. (1) into Eq. (11) yields the following equation:

\[ \Pi = p_c - \frac{\sigma_{gw}}{r - h} = (p_c - p_w)gZ \frac{\sigma_{gw}}{r - h} \] (12)

Eq. (10) can be seen as a special case of \( r = r_c \) in Eq. (12).

2.4. Relationship between disjoining pressure and water film thickness

According to the DLVO theory, the relationship between disjoining pressure and water film thickness can be expressed by the disjoining pressure isotherm. The total disjoining pressure consists of three components:

\[ \Pi = \Pi_{DLR} + \Pi_{V \Lambda} + \Pi_s \] (13)

According to Eq. (13), the relationship between the disjoining pressure \( \Pi \) and the water film thickness \( h \) at certain temperature and pressure can be calculated. After calculating the disjoining pressure \( \Pi_{eq} \) by Eq. (12), the water film thickness corresponding to the equilibrium disjoining pressure \( \Pi_{eq} \) can be determined graphically in Fig. 7.

How to calculate the three components can be as follows:

2.4.1. Electrostatic forces \( \Pi_{DLR} \)

Assuming the pore wall rock is with negative charge, Gregory [10] proposed the formula of electrostatic forces between parallel plate interfaces to calculate the electrostatic forces between gas/water interface and water/solid interface of the water film on capillary wall:

\[ \Pi_{DLR}(h) = n_A k_s T \left( \frac{2 \left[ 1 + 0.25 \left( \psi_1 + \psi_2 \right)^2 \csc h^2 \left( \frac{k h}{2} \right) \right]}{1 + 0.25 \left( \psi_1 - \psi_2 \right)^2 \exp \left( -k h \right) \csc h^2 \left( \frac{k h}{2} \right) - 2} \right) \] (14)

\[ n_A = N_A \times C, \quad \psi_1 = \frac{z e \xi}{k_s T} \] (15)

\[ \kappa = \frac{2 e^2 z^2 n_A}{\varepsilon e \varepsilon_0 k_s T} \] (16)
where $n_i$ is the ion concentration (number density) in the bulk solution, 1/m³; $k_B$ is the Boltzmann constant, the value is $1.38 \times 10^{-23}$ J/K; $T$ is the Kelvin temperature, K; $N_A$ is the Avogadro number; $C$ is the cationic molarity, mol/m³; $\Psi_s$ and $\Psi_w$ are dimensionless electrostatic potentials of gas/water interface and water/solid interface, respectively; $\lambda$ is the reciprocal of Debye length, 1/m; $\kappa$ is the dielectric constant of water, the bulk solution, 1/m³; $\varepsilon_\infty$ is the dielectric constant; $f$ is Planck constant, $6.62606896 \times 10^{-34}$ J·s; $\nu$ is the primary electronic absorption frequency in the ultraviolet region, $3 \times 10^{15}$ Hz; $n$ is refractive index.

Tokunaga [11] used the Lifshitz formula to analyze the Hamaker constant of the quartz/brine/CO₂ three-phase system at different temperatures and pressures, and obtain the value in the range of $-1.0 \times 10^{-20}$ J to $-5.6 \times 10^{-21}$ J. Hall et al. [9] recommends the Hamaker constant of the quartz/ballast/oil three-phase system with a value of $-3 \times 10^{-21}$ J to $-9 \times 10^{-21}$ J. Without considering the lag effect, Chandrasekhar and Rao [12] recommended the Hamaker constant of the quartz/saline/hydrocarbon three-phase system with a value of $-1.0 \times 10^{-20}$ J at the ground standard conditions.

2.4.3. Structure forces $\Pi_s$

It is produced by the distance between the surfaces of water film and exponential declined with the increase of the water film thickness ($h$):

$$\Pi_s (h) = A e^{-\frac{h}{\lambda_{ws}}}$$

where $A$ is the coefficient, Pa; $h$ is the characteristic decay length for the exponential model, m.

Chandrasekhar and Rao [12] recommended the Hamaker constant of the quartz/oil/oil three-phase system, because the Hamaker constant is positive, so the van der Waals force calculated from Eq. (17) is negative. For a quartz/brine/gas three-phase system, because the Hamaker constant is negative, Hirasaki [13] took the van der Waals force calculated from Eq. (17) as positive value.

2.5. Calculation method of water film thickness of pore walls in the formation

Sutton proposed to calculate the interfacial tension of gas/water interface with formula as [14]:

$$\sigma_{gw} = \frac{3.18 \times 10^{-3} \left( \rho_g - \rho_w \right) + 1.76 \left( \rho_g - \rho_w \right)^2}{T_r^{0.3125}} \times 10^{-3}$$

Eq. (21) applies only to fresh water. For formation water of high salinity, Eq. (21) should be modified as:

$$\sigma_{gw} = \frac{3.18 \times 10^{-3} \left( \rho_g - \rho_w \right) + 1.76 \left( \rho_g - \rho_w \right)^2}{T_r^{0.3125}} \times 10^{-3} + 3.44 \times 10^{-8} C_s$$

where $C_s$ is salinity, ppm; $\rho_g$ is gas density, kg/m³; $\rho_w$ is water density, kg/m³; $T_r$ is reduced temperature, dimensionless variable; $\sigma_{gw}$ is the interfacial tension between gas and water, N/m.
Eq. (12) is a function of the water film thickness. To calculate the water film thickness in pore with radius \( r \), the following methodology can be employed with iterative procedure in the following steps.

1. Calculate and draw the curve of total disjoining pressure and water film thickness as given by Eq. (13).
2. Calculate the capillary pressure \( p_c \) with Eq. (1).
3. Assuming the initial value of water film thickness is \( h = h_o \) and calculate the equilibrium disjoining pressure \( \Pi_{eq} \) with the new capillary pressure \( p_c \), interfacial tension \( \sigma_{gw} \) and the supposed pore radius \( r \):

\[
\Pi_{eq} = p_c - \frac{\sigma_{gw}}{r-h_0}
\]  

(23)

Get the \( h_0 \) value corresponding to the disjoining pressure \( \Pi_{eq} \) with graphical method as shown in Fig. 7.

4. Comparing the difference between \( h_0 \) and \( h_2 \), if it is greater than the allowable error range, make \( h_0 = h_{eq} \) and repeat steps (3) and (4), until the difference between \( h_0 \) and \( h_{eq} \) is negligible.

2.6. Water film thickness in pores at underground condition

Taking a gas reservoir in eastern China as an example, the depth of the reservoir is –2,765 m and the temperature is 130°C (403.15 K). The relative density of the natural gas is 0.56. The aqueous solution is CaCl\(_2\) solution and the water at a concentration of 6,000 ppm, or 54 mol/m\(^3\). The relative permittivity of water is 53 F/m, and the wetting contact angle is 35°. The interfacial tension of gas/water is 35 mN/m, and the relative permittivity of gas/water is 2.6.1.2. Calculation of van der Waals force

With Eq. (17), the curve of van der Waals force vs. water film thickness is shown in Fig. 9.

2.6.1.3. Calculation of structure force

With Eq. (20), the relationship between structural force and water film thickness is calculated. The calculated result shows that the structural force is small and negligible.

2.6.1.4. Calculation of water film thickness

With Eq. (13), the curve of total disjoining pressure vs. water film thickness is as shown in Fig. 10. With Eq. (1), the capillary pressure at –2,765 m in the middle of the gas reservoir is 0.1 Mpa.

Using the new water film thickness, recalculate a disjoining pressure, and the final water film thickness is still

\[
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\]

respectively. The main rock mineral is quartz and the related parameters shown in Table 1 [17]. With Eq. (19), the Hamaker constant in vacuum is \( A_{eq} = 5.96 \times 10^{-20} \text{ J} \), \( A_{se} = 2.9 \times 10^{-21} \text{ J} \), \( A_{se} = 3.59 \times 10^{-20} \text{ J} \). With Eq. (18), the Hamaker constant is \( -7.42 \times 10^{-21} \text{ J} \).

With Eq. (17), the curve of van der Waals force vs. water film thickness is shown in Fig. 9.

![Fig. 8. Relationship between electrostatic force and water film thickness.](image)

Table 1

<table>
<thead>
<tr>
<th>Material type</th>
<th>Dielectric constant ( \varepsilon )</th>
<th>Refractive index ( n )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quartz</td>
<td>3.8</td>
<td>1.448</td>
</tr>
<tr>
<td>Water</td>
<td>80.25</td>
<td>1.3333</td>
</tr>
<tr>
<td>Air</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>
2.1 nm with graphical method. It also confirms Hall’s view that the water film thickness is too small compared to pore radius, and it can be ignored directly in Eq. (6).

### 2.6.2. Influence of formation depth on water film thickness

At the depth of –2,755; –2,760 and –2,765 m, the gas and water pressure difference, or capillary pressure calculated by gas and water pressure gradients are 0.17, 0.14 and 0.1 MPa, respectively. The corresponding critical pore radius are 334.52, 422.48 and 573.2 nm, respectively.

As shown in Fig. 11, taking the pore radius is 611 nm as an example, according to Eq. (12), the equilibrium disjoining pressures in the pores of different depths are 114,129; 78,441 and 42,753 Pa, respectively.

The calculated water film thicknesses in the pores are 1.7, 1.8 and 2.1 nm, respectively. The results show that with the same pore radius, the water film thickness increases slightly with the increase of the altitude. However, the water film thickness under various conditions is relatively small compared to the pore radius (\(r > r_c\)), which is negligible.

### 2.7. Verification of water film thickness

When the disjoining pressures are \(1.5 \times 10^{-4}\) MPa and \(3.0 \times 10^{-4}\) MPa, Зорин measured the water film thicknesses of the KCl aqueous solution with 0.1 mol/m\(^3\) on the quartz plate are 100 and 75 nm, respectively [18]. Much higher than the water film thickness that calculated in the previous section.

Since the capillary bundle model used in the previous section does not apply to quartz plates, the relevant formula should be improved. If the gas/liquid/solid interface is a flat, so the curvature radius is \(R_1 = R_2 = \infty\), then Eq. (3) can be further simplified as follow:

\[
p_i = p_g - p_w = \Pi_{eq}
\]

That is:

\[
\Pi_{eq} = p_i = p_g - p_w
\]

In the water film thickness calculation method described in Section 5, the water film thickness on the quartz plate can be calculated by replacing Eq. (12) with Eq. (25).
Assuming the cationic valence is $z = 1$, and the temperature is $T = 293$ K. The zeta potential of quartz in aqueous solution under the condition of salinity is $-110$ mV [19], and the other parameters are shown in Table 1.

With Eq. (18), according to the parameters shown in Table 1, the Hamaker constant is calculated as $-9.69 \times 10^{-21}$ J. With Eq. (14), the calculation of the relationship between electrostatic forces $\Pi_{DLR}(h)$ and water film thickness is shown in Fig. 12. With Eq. (17), the calculation of the relationship between van der Waals forces and water film thickness is shown in Fig. 13. The structure forces calculated by Eq. (20) are very small and negligible.

Compared with Figs. 12 and 8, and Figs. 13 and 9, it can be seen that the decrease of electrostatic forces is larger than that of van der Waals forces after the increase of water salinity. All of this indicate that the electrostatic repulsion and the van der Waals force being the forces to keep the water film stable. When the salinity of the formation water is low, the electrostatic force and van der Waals force are the main forces to keep the water film stable.

The higher the distance from the gas/water interface, the greater the pressure difference between the gas phase and the water phase in the pores. The results of parameter sensitivity analysis show that even in the same pore radius $r$, the water film thickness in the higher position of the gas reservoir is smaller than that of the lower part due to the pressure difference of gas/water two-phase.

In the formation water with high salinity, the electrolyte compression double layer reducing the disjoining pressure between the interfaces of the water film, so the water film thickness in pores underground is small. According to the results of parameter sensitivity analysis, the bound water in the gas reservoir is mainly in the form of capillary water, and the water film thickness in the pores is much smaller than the pore radius, so the influence of water film thickness on the gas seepage process can be negligible, which is not so important as thought before.

With Eq. (13), the relationship between total disjoining pressures and water film thickness is shown in Fig. 14. When the disjoining pressures were $1.5 \times 10^{-4}$ MPa and $3.0 \times 10^{-4}$ MPa, the corresponding water film thicknesses were 83 and 67 nm, respectively. The error of the water film thickness test results in the literature was 17% and 11%.

3. Conclusions

It can be seen from the DLVO theory that in the high salinity formation aqueous solution, the structure force is negligible and the electrostatic force is small. van der Waals force is the main force to keep the water film stable. When the salinity of the formation water is low, the electrostatic force and van der Waals force are the main forces to keep the water film stable.

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Conflict of interest statement

The authors declare that there is no conflict of interest regarding the publication of this paper. We declare that we do not have any commercial or associative interest that represents a conflict of interest in connection with the work submitted.

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